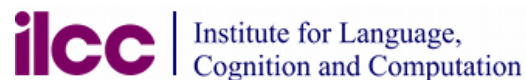


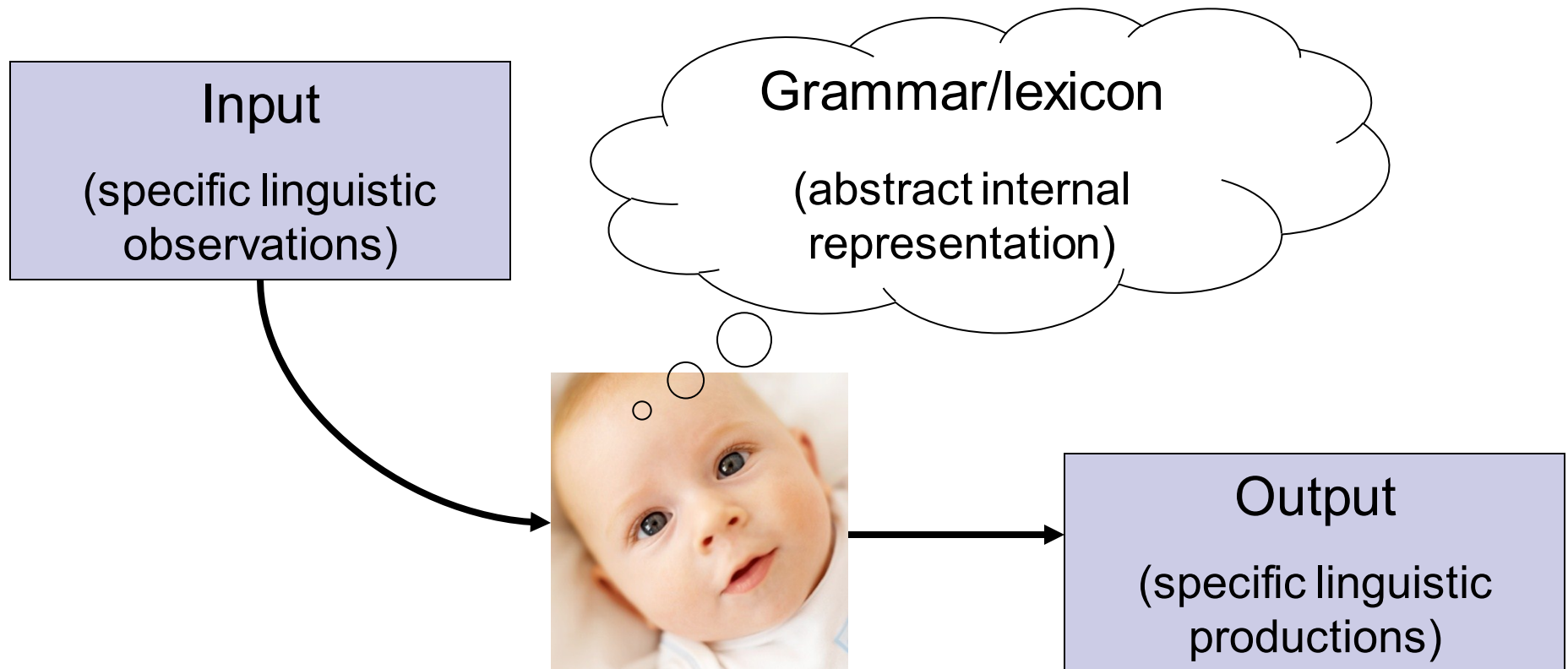
# From sounds to words: Bayesian modelling of early language acquisition.

Sharon Goldwater



THE UNIVERSITY of EDINBURGH  
**informatics**

# Language learning as induction



# Constraints on learning

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- Many generalizations are possible. What constrains the learner?
  - Innate constraints (domain-general or domain-specific).
  - Previously (or simultaneously) acquired knowledge: **bootstrapping**.
- How do these interact with each other and the input?
- How can we implement them in machines to improve coverage and accessibility of language technology?

# Modeling approach

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- Bayesian framework: a **structured probabilistic approach**.
  - Probabilistic: learner can exploit partial or uncertain information to help solve the bootstrapping problem.
  - Structured: models explicitly define representations, biases (constraints), and use of information.

# Bayesian modeling

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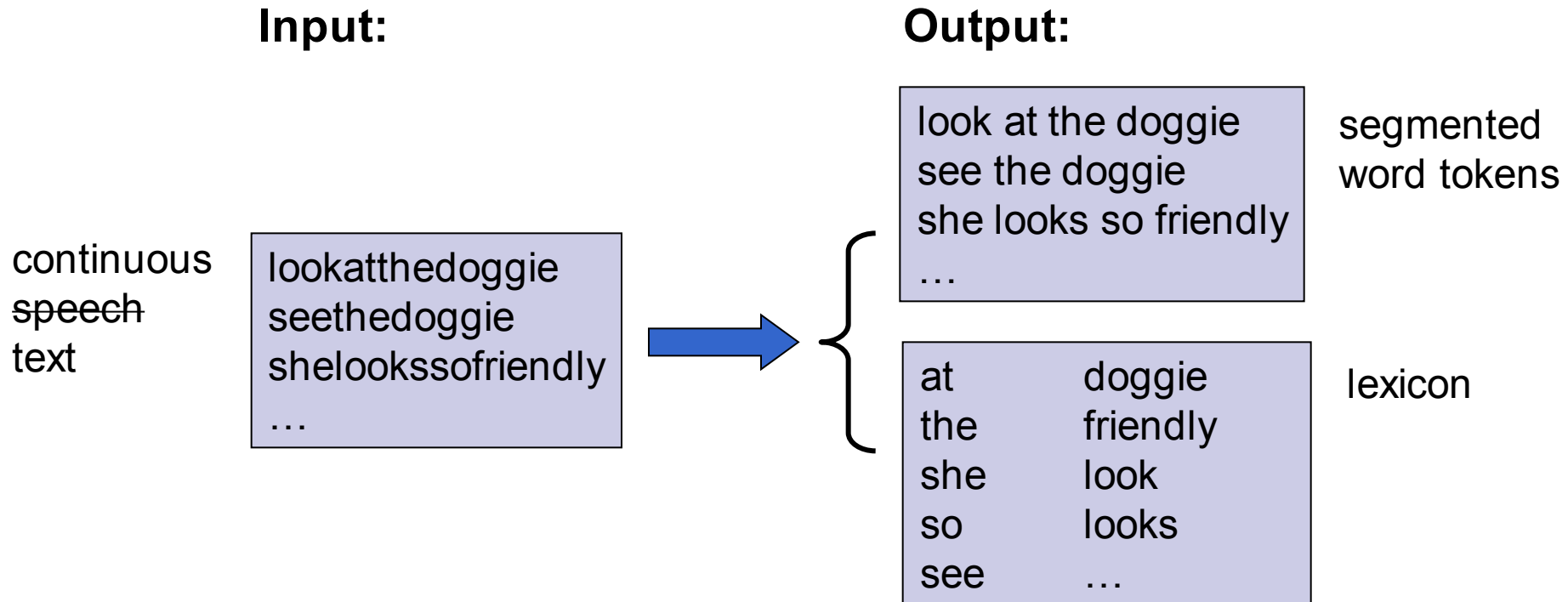
- An **ideal observer** approach.
  - What is the optimal solution to the induction problem, given particular assumptions about representation and available information?
  - In what ways might humans differ from this ideal learner, and why?

# Outline

---

1. Introduction
2. Basic model: word segmentation from phonemic input
3. Lexical-phonetic learning from phonetic input
4. Word extraction from acoustic input

# Word segmentation (idealized)



# Research questions

---

- Machine learning:

- ☐ Can we develop a generative probabilistic model and effective inference method to discover the words?
- ☐ I.e., can we learn an n-gram language model without knowing the words in advance?

- Cognitive science:

- ☐ What kinds of assumptions must a learner make in order to discover words correctly?
- ☐ Is a simple unigram model sufficient?

# Bayesian learning

- Formulate the problem as a Bayesian model:

$$\underbrace{P(h|d)}_{\text{posterior}} \propto \underbrace{P(d|h)}_{\text{likelihood}} \underbrace{P(h)}_{\text{prior}}$$

- Focus is on the goal of the computation rather than on using a cognitively plausible learning algorithm.

## Data:

lookatthedoggie  
seethedoggie  
shelookssofriendly  
...

## Hypotheses:

lookatthedoggie  
seethedoggie  
shelookssofriendly  
...

lookatthedoggie  
seethedoggie  
shelookssofriendly  
...

look at thed oggi e  
se e thed oggi e  
sh e look ssofri e ndly  
...

look at the doggie  
see the doggie  
she looks so friendly  
...

i like pizza  
what about you  
...

abc def gh  
ijklmn opqrst uvwx  
...


$$P(d|h)=1$$

$$P(d|h)=0$$

# Bayesian segmentation

- For segmentation,
  - Data: unsegmented corpus (transcriptions).
  - Hypotheses: sequences of word tokens.
- Under phonemic assumption, the prior does all the work.

$$\underbrace{P(h|d)}_{\text{posterior}} \propto \underbrace{P(d|h)}_{\text{likelihood}} \underbrace{P(h)}_{\text{prior}}$$

= 1 if concatenating words forms corpus,  
= 0 otherwise.

Encodes assumptions of  
learner.

# Unigram model

- Assume words are drawn from Dirichlet Process. Then

$$P(w_{n+1} = w \mid w_1 \dots w_n) = \frac{n_w + \alpha P_0(w)}{n + \alpha}$$

with  $P_0(w = x_1 \dots x_m) = \prod_{i=1}^m P(x_i)$  for characters  $x_1 \dots x_m$ .

- “Rich-get-richer” process creates Zipfian distribution.
- **Base distribution**  $P_0$  favors shorter lexical items.
- Number of lexical items grows with data size.
- Probabilities don’t depend on immediate context: unigram model.

# Bigram model

- Assume words are drawn from hierarchical Dirichlet process.

$$P(w_{n+1} = w \mid w_n = w', w_1 \dots w_{n-1}) = \frac{n_{(w',w)} + \beta P_1(w)}{n_{w'} + \beta}$$

$$P_1(w_{n+1} = w \mid w_1 \dots w_n) = \frac{b_w + \alpha P_0(w)}{b + \alpha}$$

- Similar assumptions to unigram model, but now words also depend on context.

# Experiments

- Inference: simple Gibbs sampler.
  - Other methods possible (Mochihashi et al., 2009; Liang and Jordan 2010).
- Corpus:
  - 9790 utterances of phonemically transcribed child-directed speech (19-23 months).
  - Average 3.4 words/utterance, 2.9 phonemes/word.

```
yuwanttusID6bUk  
lUkD*z6b7wIThIzh&t  
&nd6dOgi  
yuwanttulUk&tDI s  
...
```

# Example results

## Unigram model

```
youwant to see thebook  
look theres aboy with his hat  
and adoggie  
you wantto lookatthis  
lookatthis  
havea drink  
okay now  
whatsthis  
whatsthat  
whatisit  
look canyou take itout  
...
```

## Bigram model

```
you want to see the book  
look theres a boy with his hat  
and a doggie  
you want to lookat this  
lookat this  
have a drink  
okay now  
whats this  
whats that  
whatis it  
look canyou take it out  
...
```

# Conclusions

---

- Good segmentations of (phonemic) data can be found using fairly weak prior assumptions.
  - Utterances are composed of discrete units (words).
  - Units tend to be short.
  - Some units occur frequently, most do not.
  - Units tend to come in predictable patterns; i.e. context is key.

# Further tests

---

- Frank, Goldwater, Griffiths, and Tenenbaum (2010):
  - Model captures human performance in an artificial segmentation task better than all other models tested.
- Pearl, Goldwater, and Steyvers (2010):
  - Incremental (but non-optimal) algorithms can sometimes yield more accurate results than batch versions.
  - Can “burstiness” be used to our advantage (as humans, or to design more efficient computer algorithms)?

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---

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# Phones and words

- Most models of word segmentation use **phonemic** input.

(a) intended:            /ju want wʌn/    /want e kʊki/

(d) idealized:            /juwantwʌn/    /wantekʊki/

# Phones and words

- Abstracts away from phonological and phonetic variation.

|                  |               |               |
|------------------|---------------|---------------|
| (a) intended:    | /ju want wʌn/ | /want e kʊki/ |
| (b) surface:     | [jə wãʔ wʌn]  | [wan ə kʊki]  |
| (c) unsegmented: | [jəwãʔwʌn]    | [wanəkʊki]    |
| (d) idealized:   | /juwantwʌn/   | /wantekʊki/   |

- But: phonological and word learning occur simultaneously and seem to interact.
  - How can we model this kind of **joint learning**? Will model predictions change?

# Joint learning

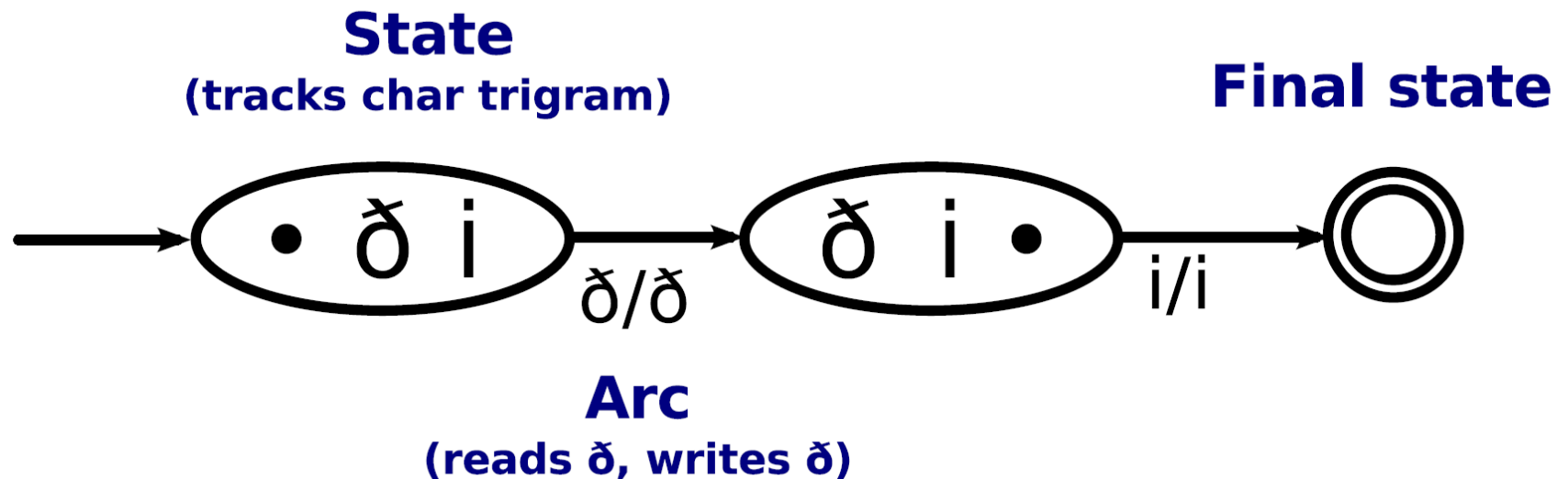
|               |               |               |
|---------------|---------------|---------------|
| (a) intended: | /ju want wʌn/ | /want e kʊki/ |
| (b) surface:  | [jə wãʔ wʌn]  | [wan ə kʊki]  |

- Here: From surface forms, learn a lexicon, a language model, and a model of phonetic variation.
- Method: (unsupervised) noisy channel model.
  - Language model: similar to GGJ09.
  - Phonetic model: MaxEnt model using articulatory features.

# Phonetic model

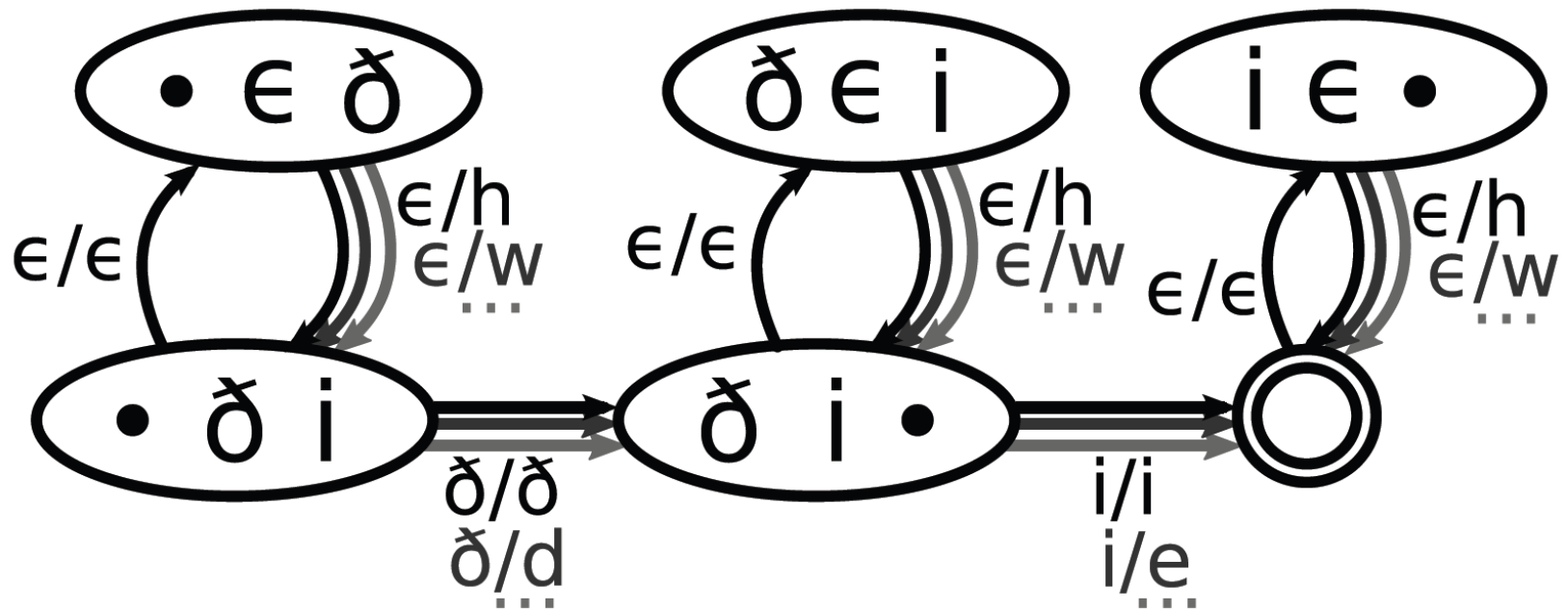
- Implemented as weighted finite-state transducer. Ex:

**Identity FST given ỗi**  
(reads ỗi "the" and writes ỗi)



# Our transducer

Reads ði, writes anything  
(Likely outputs depend on parameters)



- Prob. of arc depends on features of sounds (same/different voicing/place/manner, etc.). Weights are learned.

# Results so far (Elsner, Goldwater, and Eisenstein, 2012)

- Inference: approximate method greedily merges surface forms, retrains transducer after each merging pass.
- Data: simulate phonetic variation in BR corpus by sampling phonetic forms from Buckeye corpus.

“about”      ahbawt:15, bawt:9, ihbawt:4, ahbawd:4, ih-  
bawd:4, ahbaat:2, baw:1, ahbaht:1, erbawd:1,  
bawd:1, ahbaad:1, ahpaat:1, bah:1, baht:1,  
ah:1, ahbahd:1, ehbaat:1, ahbaed:1, ihbaht:1,  
baot:1

# Results so far (Elsner, Goldwater, and Eisenstein, 2012)

- Inference: approximate method greedily merges surface forms, retrain transducer after each merging pass.
- Data: simulate phonetic variation in BR corpus by sampling phonetic forms from Buckeye corpus.
- Results:

|            | Token F | Lexicon F |
|------------|---------|-----------|
| Baseline   | .65     | .67       |
| Unigram LM | .75     | .76       |
| Bigram LM  | .79     | .87       |

# What about segmentation?

- System also improves lexicon when using inferred word boundaries (from GGJ09).
- But:
  - Overall performance much worse (.44 → .49 vs. .65 → .79).
  - Iterating segmentation and lexicon learning doesn't help.
- In progress: new system with beam sampler instead of greedy search, simultaneously learns segmentation.

# Conclusions

---

- First joint model of phonetic and word learning using word-level context info on phonetic corpus data.
- Additional evidence that word and phone learning can inform each other.
- As in phonemic model, word-level context is important—helps disambiguate similar-sounding words (e.g., what/wet).
- Dealing with segmentation ambiguity also is hard.

# Outline

---

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# Learning words from acoustics

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- Goal: investigate incremental (online) learning in a model of whole-word extraction from speech.
- Method: modify Park and Glass (2008) algorithm to be (more) incremental.

# Algorithm

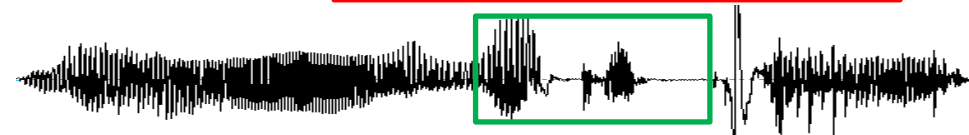
1. Compare pairs of utterances to extract pairs of acoustically similar speech fragments:



*Look at the doggie*



*Where's the doggie*

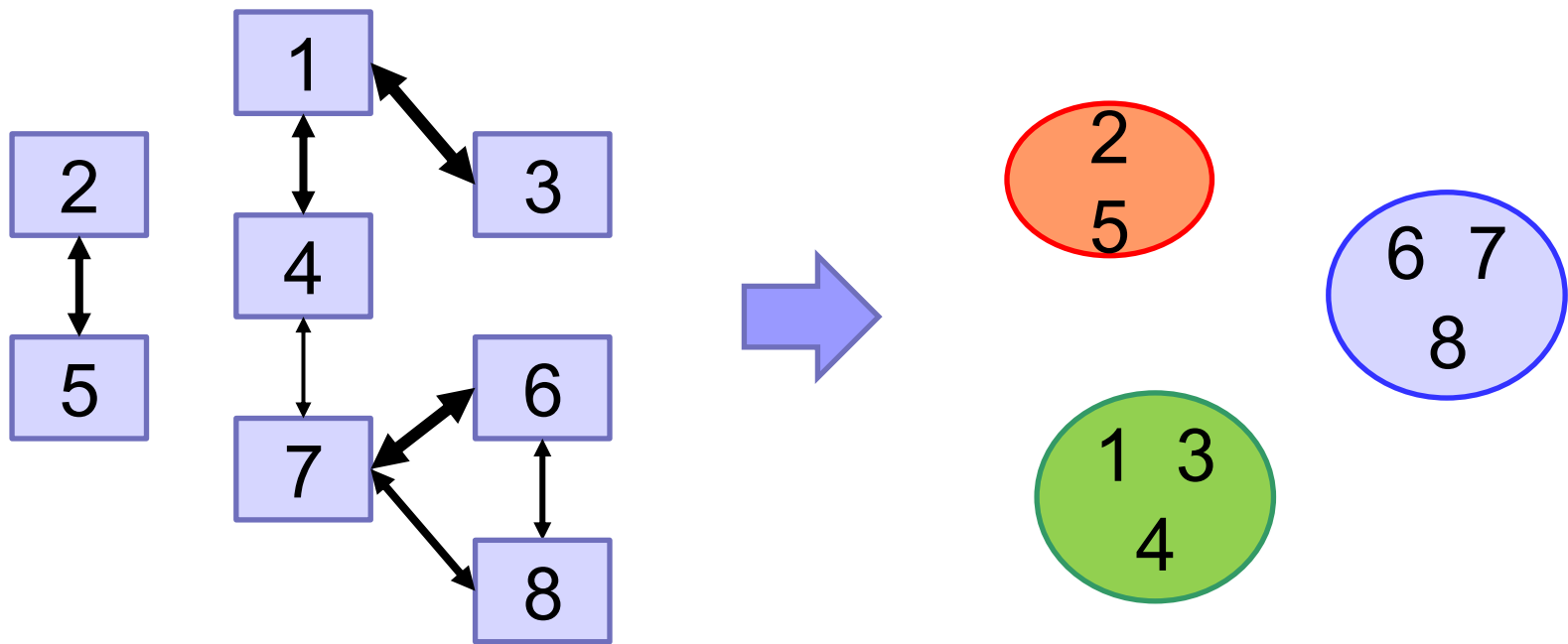


*Yeah, look at that*

- Uses a slightly modified version of P&G's Segmental DTW.
- Compares only with fixed-size window of utterances.

# Algorithm:

2. Cluster together extracted fragments pairs into larger groups: lexical items.



# Experiments:

---

- Test on recordings from parents of 9-15 month-olds.
- Measure *entropy reduction* and examine words found.
- Results:
  - Original corpus: Little difference between using limited window (10-20 utterances) or full batch mode.
  - Permuted corpus: Limited window results are much worse.
  - 'Mommy' and child's name are found in most sessions.

# Conclusions

---

- Frequent nearby repetitions are helpful to the incremental learner: limited memory is almost as good as batch learning.
- Simple pattern-matching can extract word-like units, but boundaries not always accurate.
- Open issues:
  - Online clustering method.
  - Relationship between these units and sub-word units.
  - Word extraction vs. word segmentation.

# Issues/ideas for future work

- Extending Bayesian models to work from acoustics.
  - Lee & Glass (2012) a great start on phonetic clustering; can we build in higher-level dependencies and learn a lexicon?
  - Consider intermediate levels of representation (syllables).
- Developing better inference methods.
  - Efficient for machine learning; cognitively plausible for human models.
  - Can we exploit structure that isn't captured by our generative models (e.g., burstiness) to design better inference methods? (Or should we design more accurate models?)
- Using non-acoustic information (e.g., articulatory gestures, visual context, gesture).





# Bayesian model

Assumes word  $w_i$  is generated as follows:

1. Is  $w_i$  a novel lexical item?

$$P(yes) = \frac{\alpha}{n + \alpha}$$

$$P(no) = \frac{n}{n + \alpha}$$

Fewer word types =  
Higher probability

# Bayesian model

Assume word  $w_i$  is generated as follows:

2. **If novel**, generate phonemic form  $x_1 \dots x_m$  :

$$P(w_i = x_1 \dots x_m) = \prod_{i=1}^m P(x_i)$$

Shorter words =  
Higher probability

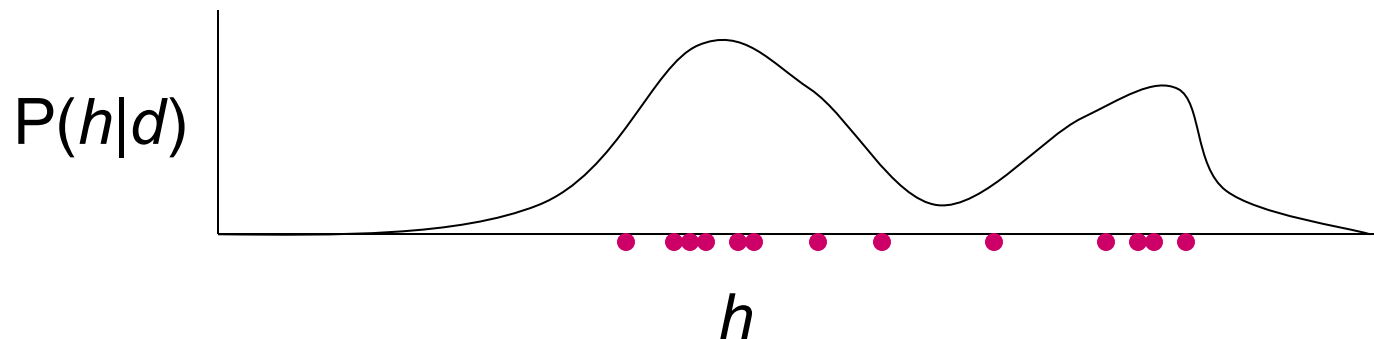
**If not**, choose lexical identity of  $w_i$  from previously occurring words:

$$P(w_i = w) = \frac{n_w}{n}$$

Power law =  
Higher probability

# Learning algorithm

- Model defines a distribution over hypotheses. We use **Gibbs sampling** to find a good hypothesis.
  - Iterative procedure produces samples from the posterior distribution of hypotheses.



- A batch algorithm, assumes perfect memory for data.

# Inference

- We use a Gibbs sampler that compares pairs of hypotheses differing by a single word boundary:

```
whats . that  
the . doggie  
yeah  
wheres . the . doggie  
...
```

```
whats . that  
the . dog . gie  
yeah  
wheres . the . doggie  
...
```

- Calculate the probabilities of the words that differ, given current analysis of all other words.
- Sample a hypothesis according to the ratio of probabilities.

# Incremental Sampling

For each utterance:

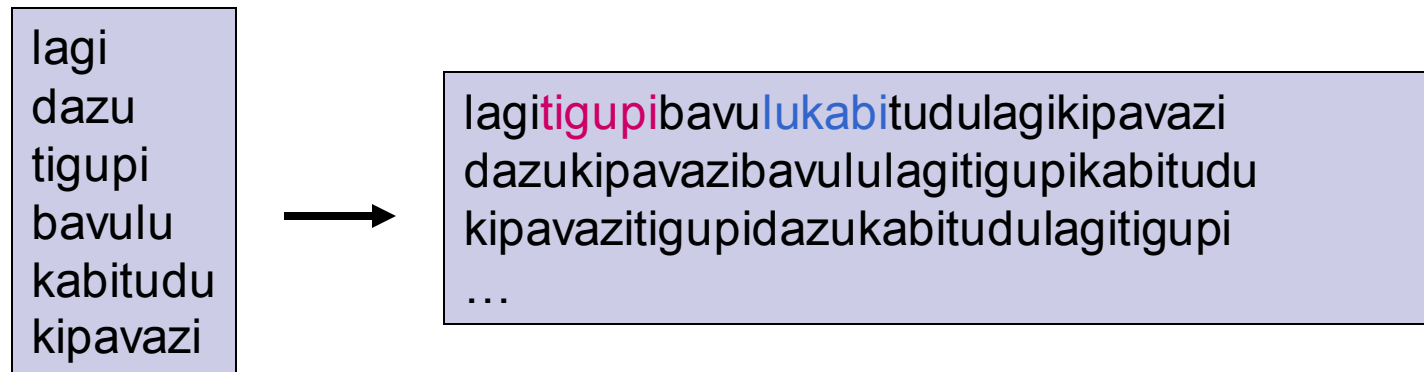
- Sample a segmentation from the posterior distribution given the current lexicon.
- Add counts of segmented words to lexicon.

- Online algorithm
- Limits memory for corpus data

(Particle filter: more particles  $\Leftrightarrow$  more memory)

# Testing model predictions

- Saffran-style experiment using multiple utterances.
  - Synthesize stimuli with 500ms pauses between utterances.



- Training: adult subjects listen to corpus of utterances.
  - Testing: 2AFC between **words** and **part-word** distractors
- Compare our model (and others) to humans, focusing on changes in performance as task difficulty is varied.

# Experiment 1: utterance length

- Vary the number of words per utterance.

| #vocab | # wds/utt | # utts | tot # wds |
|--------|-----------|--------|-----------|
| 6      | 1         | 1200   | 1200      |
| 6      | 2         | 600    | 1200      |
| 6      | 4         | 300    | 1200      |
| 6      | 6         | 200    | 1200      |
| 6      | 8         | 150    | 1200      |
| 6      | 12        | 100    | 1200      |



# Experiment 2: exposure time

- Vary the number of utterances heard in training.

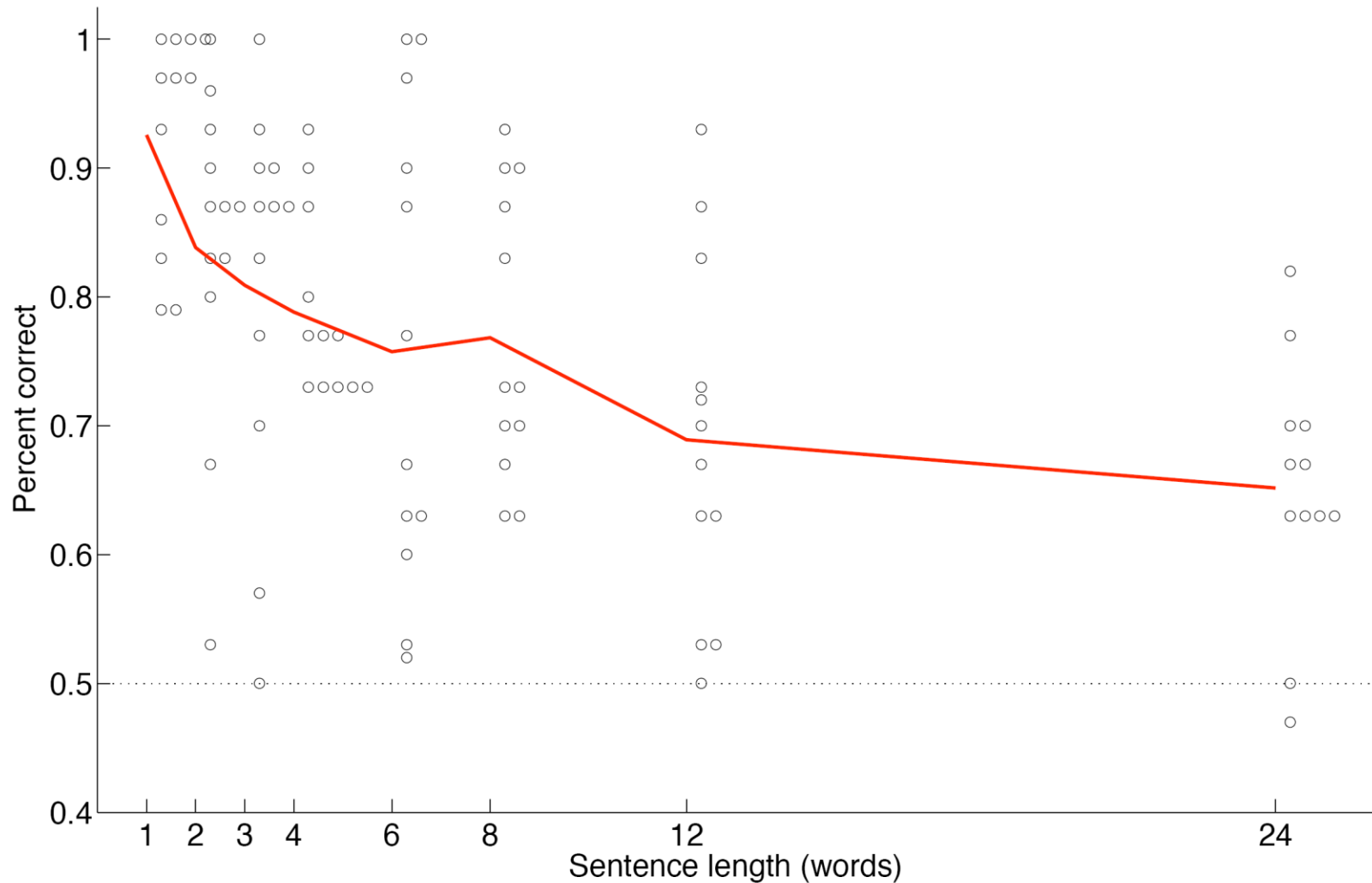
| #vocab | # wds/utt | # utts | tot # wds |
|--------|-----------|--------|-----------|
| 6      | 4         | 12     | 48        |
| 6      | 4         | 25     | 100       |
| 6      | 4         | 75     | 300       |
| 6      | 4         | 150    | 600       |
| 6      | 4         | 225    | 900       |
| 6      | 4         | 300    | 1200      |

# Experiment 3: vocabulary size

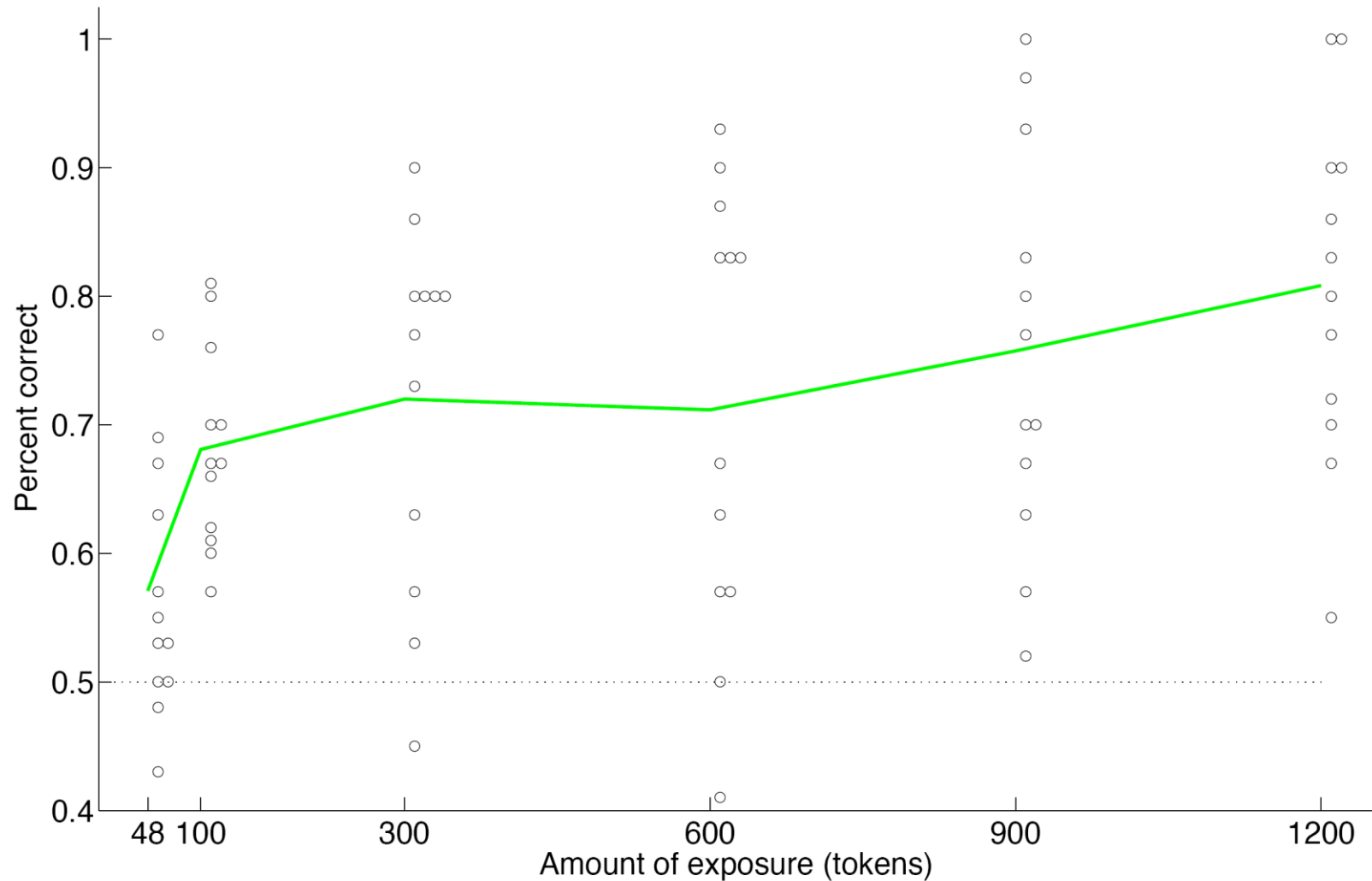
- Vary the number of lexical items.

| #vocab | # wds/utt | # utts | tot # wds |
|--------|-----------|--------|-----------|
| 3      | 4         | 150    | 600       |
| 4      | 4         | 150    | 600       |
| 5      | 4         | 150    | 600       |
| 6      | 4         | 150    | 600       |
| 9      | 4         | 150    | 600       |

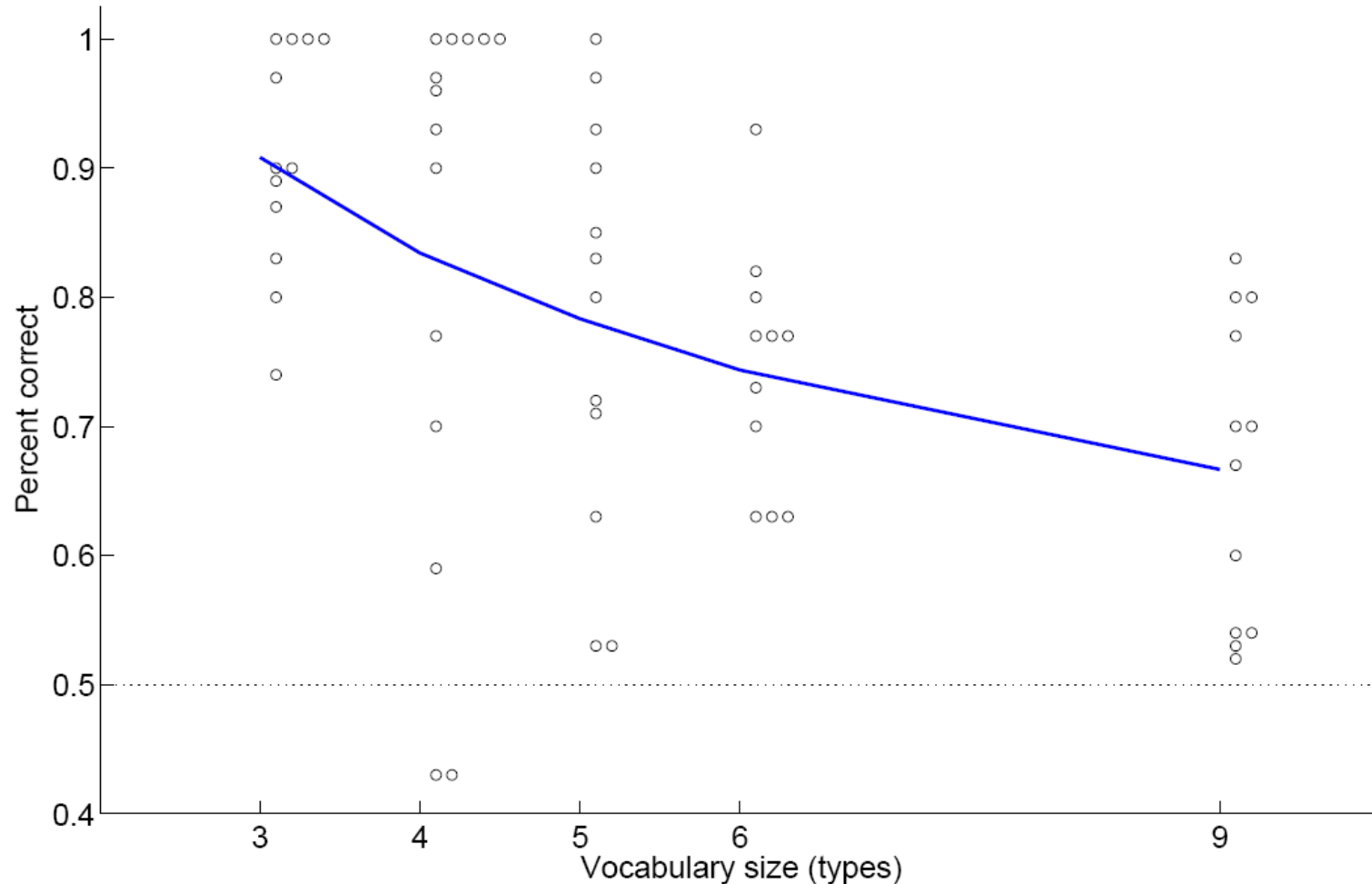
# Human results: utterance length



# Human results: exposure time



# Human results: vocabulary size



# Model comparison

- Evaluated six different models.
- Each model trained and tested on same stimuli as humans.
- For testing, produce a score  $s(w)$  for each item in choice pair and use Luce choice rule:

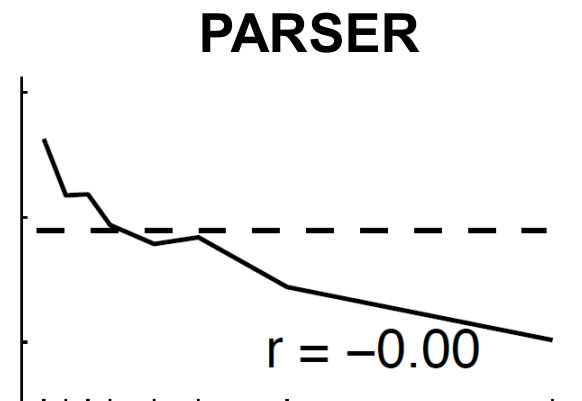
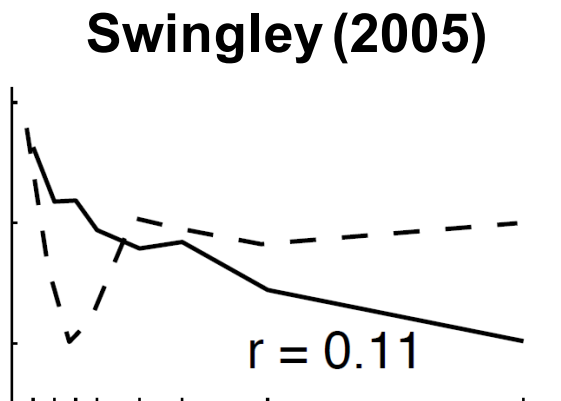
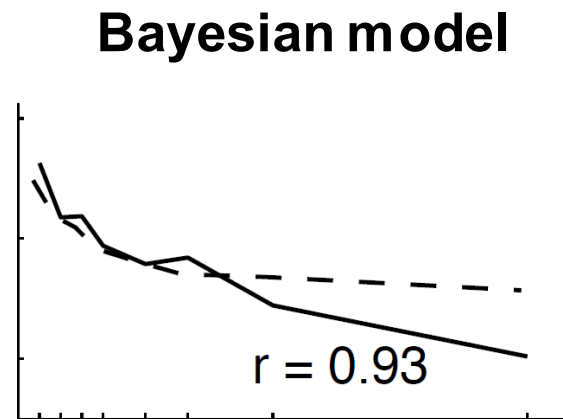
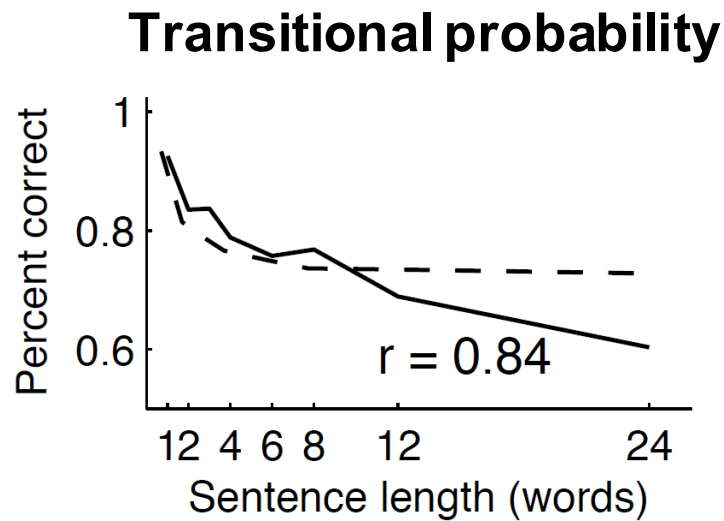
$$P(w_1) = \frac{s(w_1)}{s(w_1) + s(w_2)}$$

- Calculate correlation coefficients between each model's results and the human data.

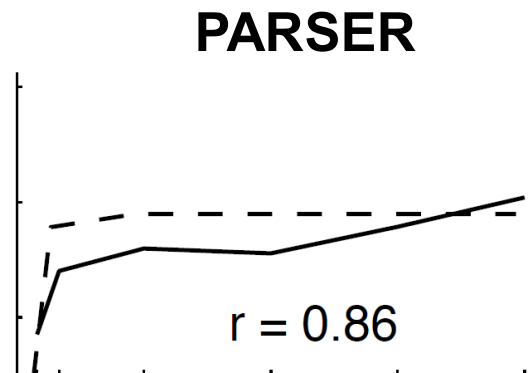
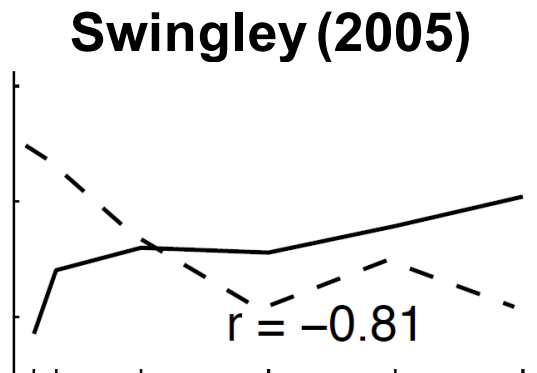
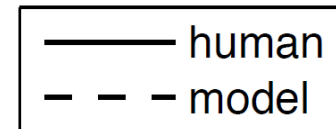
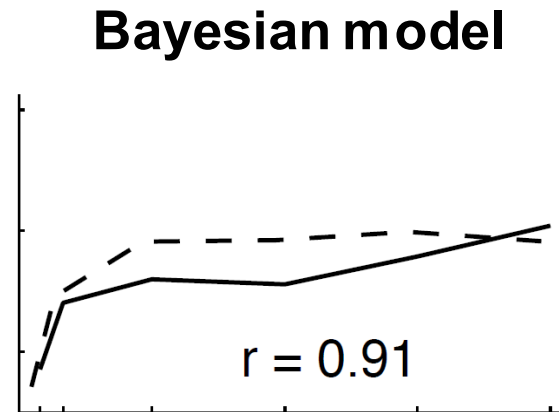
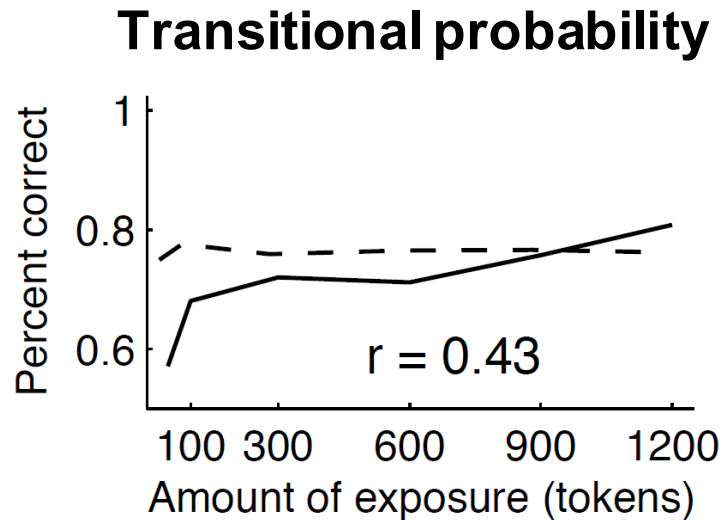
# Models used

- Several variations on transitional probabilities (TP)
  - $s(w)$  = minimum TP in  $w$ .
- Swingley (2005)
  - Builds lexicon using local statistics and frequency thresholds.
  - $s(w)$  = max threshold at which  $w$  appears in lexicon.
- PARSER (Perruchet and Vintner, 1998)
  - Incorporates principles of lexical competition and memory decay.
  - $s(w) = P(w)$  as defined by model.
- Bayesian model
  - $s(w) = P(w)$  as defined by model.

# Results: utterance length



# Results: exposure time



# Summary: Experiments 1 and 2

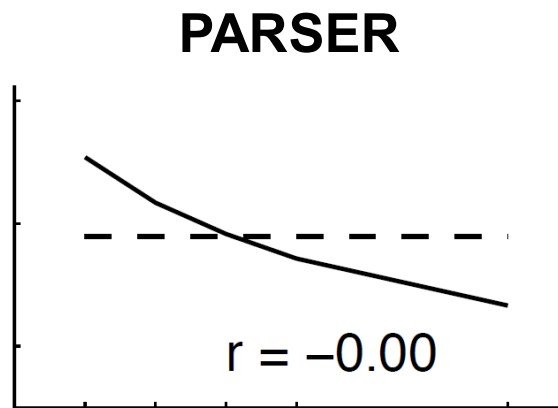
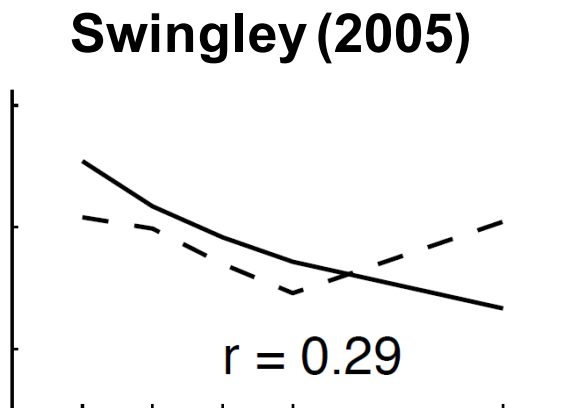
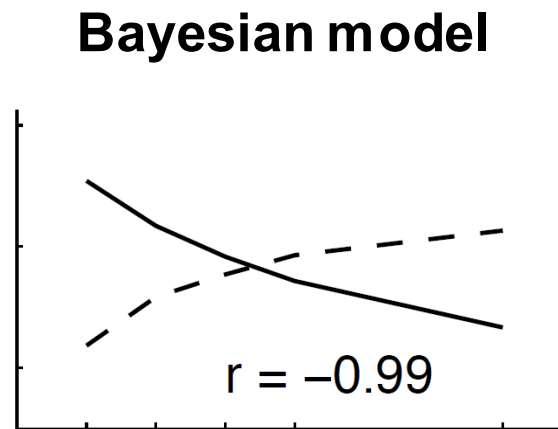
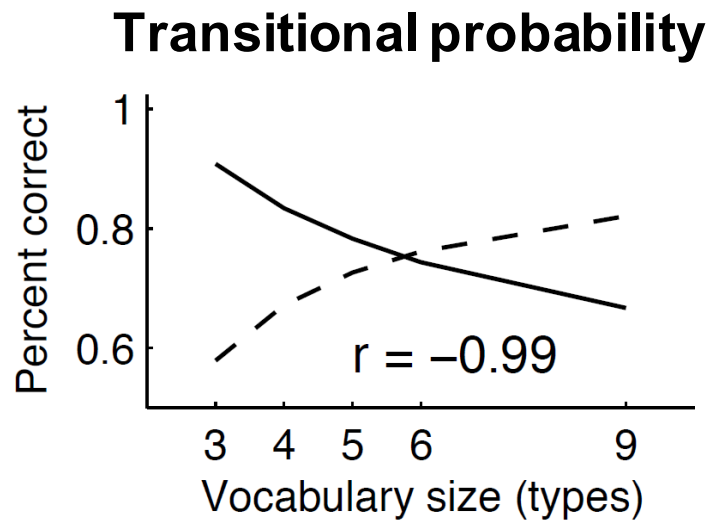
- For humans, learning to segment is more difficult
  - when utterances contain more words.
  - when less data is available.

- Only Bayesian model captures both effects:

|            | TPs | Sw05 | PARSER | Bayes |
|------------|-----|------|--------|-------|
| Utt length | ✓   | ×    | ×      | ✓     |
| Exposure   | ×   | ×    | ✓      | ✓     |

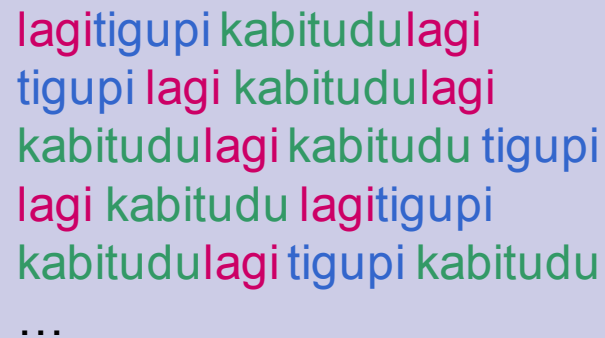
- Success is due to accumulation of **evidence** for best hypothesis, moderated by **competition** with other hypotheses.

# Model results: vocabulary size



# What's going wrong?

- TPs: smaller vocab => TPs across words are higher.
- Bayes: smaller vocab => Incorrect solutions have relatively small vocabularies with many frequent “words”.



lagitigupi kabitudulagi  
tigupi lagi kabitudulagi  
kabitudulagi kabitudu tigupi  
lagi kabitudu lagitigupi  
kabitudulagi tigupi kabitudu  
...

- With perfect memory, stronger statistical cues of larger vocabulary outweigh increased storage needs.

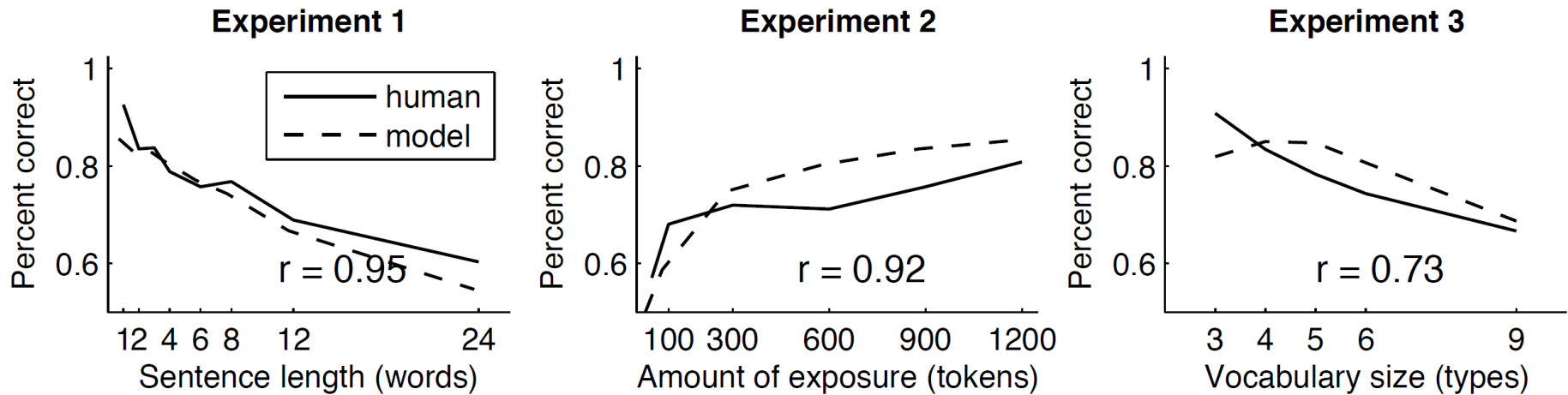
# Memory limitations

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- Modified Bayesian model has limited memory for data and generalizations.
  - Online learning algorithm processes one utterance at a time, one pass through data.
  - Random decay of items in lexicon.
- Learner is no longer guaranteed to find optimal solution.

# Results: memory-limited learner

- Good fit to all three experiments:



- Simulating limited memory in TP also improves results but not as much.

# Summary

---

- Humans behave like ideal learners in some cases.
  - Longer utterances are harder – competition.
  - Shorter exposure is harder – less evidence.
- Humans are unlike ideal learners in other cases.
  - Larger vocabulary is harder for humans, easier for model.
- Memory-limited learner captures human behavior in all three experiments.

# Targets vs. distractors

Transitional Probability  
Lexical model

