

# Confidence Based Lattice Segmentation and Minimum Bayes-Risk Decoding

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## Introduction

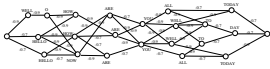
- Minimum Bayes Risk (MBR) decoders have shown improvements over MAP decoders using N-best List Rescoring and  $A^*$  search over word lattices.
- Segmental MBR decoders simplify implementation of MBR decoders by segmenting the N-best lists or Lattices.
- We present:
  - A method to segment Word Lattices into regions of low confidence and high confidence.
  - Three SMBR procedures that can be applied on low confidence segment sets.
  - Results on the SWITCHBOARD speech corpus showing error rate improvements with SMBR decoding.

## 1 Minimum Bayes-Risk Speech Recognizers

- Minimum Bayes-risk (MBR) decoder on an utterance  $A$ :

$$\delta(A) = \operatorname{argmin}_{W' \in \mathcal{W}_1} \sum_{W \in \mathcal{W}_2} l(W, W') P(W|A)$$

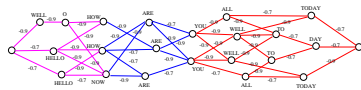
- A word lattice



- N-best rescoring<sup>1</sup> or lattice based  $A^*$ <sup>2</sup> implementations.

## 2 Segmental Minimum Bayes-Risk (SMBR) Decoders

- A segmented word lattice



- We want to obtain a segmentation such that:

$$l(W, W') = l(W_1, W'_1) + l(W_2, W'_2) + l(W_3, W'_3)$$

- Segmental MBR decoder is a concatenation of MBR decoders:

$$\delta(A) = \begin{cases} \operatorname{argmin}_{W' \in \mathcal{W}_1} \sum_{W \in \mathcal{W}} l(W, W') P_1(W|A) \\ \operatorname{argmin}_{W' \in \mathcal{W}_2} \sum_{W \in \mathcal{W}} l(W, W') P_2(W|A) \\ \operatorname{argmin}_{W' \in \mathcal{W}_3} \sum_{W \in \mathcal{W}} l(W, W') P_3(W|A) \end{cases}$$

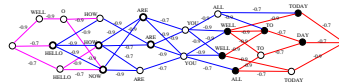
## 3 Issues in the SMBR Approach

- Primary benefit of SMBR is reduction in search space: A large search problem is broken down into many smaller search problems.
- SMBR decoder generates hypotheses not present in original lattice.
- SMBR involves tradeoff between search errors (no segmentation) and errors in loss function approximation.
- We have developed Lattice Cutting as a procedure that segments a word lattice into low confidence and high confidence regions.
- Segmentation restricts the possible string alignments:
  - We want the induced loss due to the segmentation to approximate the desired loss function.

$$l(W, W') \approx \sum_{i=1}^N l(W_i, W'_i)$$

## 4 A Lattice Cutting Method Based on Node Sets

- Cutting a lattice based on  $N_s$  and  $N_e$



- How to select Node Sets  $N_s$  and  $N_e$ ?
  - Along each path in  $\mathcal{W}$ , there needs to be at least one node in  $N_s$  and one node in  $N_e$
  - Nodes of  $N_s$  precede nodes of  $N_e$  on that path
- Need to compute marginal probabilities of paths in the lattice segment  $W_i$ 
  - Marginal probabilities should be computed over longest sub-paths in  $W_i$

## 5 Marginal Probabilities of Paths in Lattice Cuts

- Goal: To compute  $P_i(W_i|A)$ , the marginal probability of word string  $W_i$  in Lattice segment  $W_i$

- Lattice Forward Probability of the first node  $n_1$  of  $W_i$ ,  $n_1 \in N_s$ :

$$F(n_1) = \sum_{W_p: E^l(W_p)=n_1} e^{L_f(W_p)}$$

Notation:

- $W_p$  is a prefix of a lattice path  $W$
- $E^l(W_p)$ : Last Node of  $W_p$
- $L_f(W_p)$ : Joint acoustic and language model log-likelihood of  $W_p$
- $E(W_p)$ : All lattice nodes through which  $W_p$  passes

- Define a Restricted Lattice Forward Probability of node  $n_1$

$$F(n_1; N_s) = \sum_{W_p: E^l(W_p)=n_1} e^{L_f(W_p)} \mathbb{1}_{E(W_p) \cap N_s = \{n_1\}}$$

- For a node  $n_1 \in N_s$ , Lattice Paths that pass through a node of  $N_s$  before  $n_1$  contribute a segment longer than  $W_i$  to  $W_i$ . Their probabilities are to be excluded.

- Lattice Backward Probability of the final node  $n_2$  of  $W_i$ ,  $n_2 \in N_e$

$$B(n_2) = \sum_{W_s: E^h(W_s)=n_2} e^{L_b(W_s)}$$

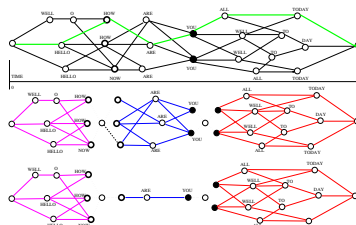
Notation:

- $W_s$  is a suffix of a lattice path  $W$
- $E^h(W_s)$  is the starting node of  $W_s$
- $L_b(W_s)$  is the joint acoustic and language model log-likelihood of  $W_s$  conditioned on starting node of  $W_s$ .

- Marginal Probability of string  $W_i$  in section  $i$ :

$$P_i(W_i|A) = \frac{F(n_1; N_s) P(W_i, A|W_i) B(n_2)}{P(A)}$$

## 6 A Confidence Based Lattice Cutting Procedure



## 7 SMBR decoding of Lattice Cuts

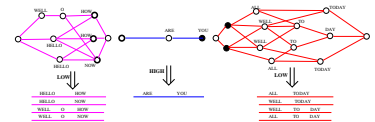
- Three MBR decoding procedures on lattice cuts
  - $A^*$  search
  - N-best list rescoring
  - Lattice Cutting E-ROVER (LCER)
- For  $A^*$  search and N-best List rescoring, MBR decoding on a lattice cut  $W_i$ :

$$\hat{W}_i = \operatorname{argmin}_{W'_i \in \mathcal{W}_1} \sum_{W_i \in \mathcal{W}_2} l(W_i, W'_i) P_i(W_i|A)$$

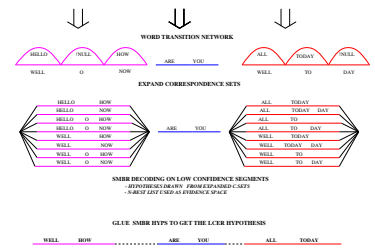
- For LCER, the search and the sum are over different spaces

## 8 Lattice Cutting E-ROVER

- Evidence Space Generation



- Hypothesis Space Generation



## 9 Results on SWITCHBOARD

- Johns Hopkins University Hub-5 LVCSR 2001 Evaluation System.

- Test sets: Swbd2-portion of 1998 evalset (swbd2-98), Swbd1-portion of 2000 evalset (swbd1-00) and 2001 evalsets (swbd1-01, swbd2-01, swbd2cell-01)

- SMBR Methods: N-Best List Rescoring and E-ROVER

Decoding Strategy	WER			
	swbd2-98	swbd1-00	swbd1-01	swbd2-cell-01
MAP (baseline)	41.1	26.0	26.8	37.7
N-best rescoring	40.4	25.6	26.6	37.2
Lattice cutting	40.2	25.4	-	-
e-ROVER	40.5	25.7	-	-
Lattice cutting	40.0	25.2	26.5	31.5

- Results Not Included in JHU 2001 Evaluation

- Test Set: The 1997 JHU LVCSR workshop test set
- SMBR Procedures: N-Best List Rescoring and  $A^*$  decoding

Decoding Strategy	WER
	MAP (baseline)
N-best rescoring	37.9
$A^*$ search	37.5
Lattice cutting	37.1

## 10 Conclusions and Future Work

- A lattice cutting procedure that segments lattices into regions of low and high confidence
- Three procedures for MBR decoding on segmented lattices
- Performance of MBR procedures improves when applied to lattice cuts
- Ongoing Research
  - Improved lattice segmentation: not relying on time information
  - $A^*$  search procedures with separate hypothesis and evidence spaces

<sup>1</sup>A. Stolcke, Y. Konig, and M. Weintraub, "Explicit word error minimization in N-best list rescoring," Eurospeech-97, pp. 163-165, Rhodes, Greece, 1997.  
<sup>2</sup>V. Goel and W. Byrne, "Minimum Bayes-risk automatic speech recognition," Computer Speech and Language, Vol. 14(2), pp. 115-135, 2000.